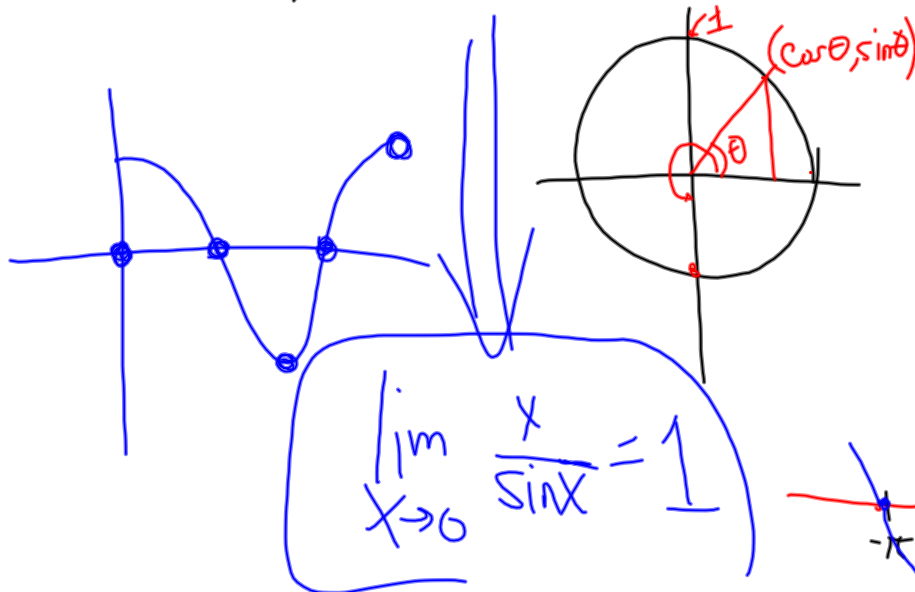


2.6/28

$$\lim_{x \rightarrow 0} \frac{x}{\cos(\frac{\pi}{2} - x)}$$

sin

x	$\frac{\pi}{2} - x$
$-\pi$	2π $\frac{3\pi}{2}$
$-\frac{\pi}{2}$	π
0	$\frac{\pi}{2}$
$\frac{\pi}{2}$	0
π	$-\frac{\pi}{2}$
\vdots	



$$\cos(x \pm y) = \cos x \cos y \mp \sin x \sin y$$

$$\begin{aligned} \cos\left(\frac{\pi}{2} - x\right) &= \cos\frac{\pi}{2} \cos x + \sin\frac{\pi}{2} \sin x \\ &= 0 + (1) \sin x \end{aligned}$$

$$\lim_{h \rightarrow 0} \frac{\sin h}{1 - \cos h} = \lim_{h \rightarrow 0} \left(\frac{\sin h}{h} \right) \left(\frac{h}{1 - \cos h} \right)$$

= DNE!

1

"1"
~ 0

$$\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$$

$$\lim_{x \rightarrow 0} \frac{1 - \cos x}{x} = 0$$

$$\lim_{h \rightarrow 0^+} \text{wavy} = +\infty$$

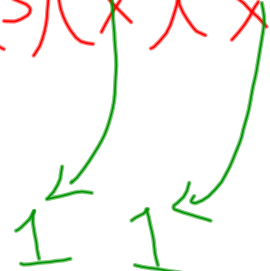
$$\lim_{h \rightarrow 0^-} \text{wavy} = -\infty$$

$$\lim_{h \rightarrow 0} \frac{\sin h}{1 - \cos h}$$

$$\lim_{h \rightarrow 0} \frac{\sin h}{(1 - \cosh)} \cdot \frac{(1 + \cosh)}{(1 + \cosh)} = \lim_{h \rightarrow 0} \frac{\sin h (1 + \cosh)}{1 - \cos^2 h}$$

$$= \lim_{h \rightarrow 0} \frac{(\sin h) \cdot (1 + \cosh)}{(\sin h) \cdot \sin h} \Rightarrow DNE$$

~~XX~~

$$\lim_{x \rightarrow 0} \frac{\sin^2 x}{3x^2} = \lim_{x \rightarrow 0} \left(\frac{1}{3} \right) \left(\frac{\sin x}{x} \right) \left(\frac{\sin x}{x} \right)$$


$$\frac{\cancel{IX}}{II}$$

$$\lim_{t \rightarrow 0} \frac{t^2}{1 - \cos^2 t}$$

$$= \lim_{t \rightarrow 0} \frac{t^2}{\sin^2 t} = \frac{1}{\lim_{t \rightarrow 0} \frac{\sin^2 t}{t^2}} = 1$$

3.1) WHAT U KNOW

Average Speed = $\frac{\text{change in distance}}{\text{change in time}}$



average velocity = $\frac{\text{change in position}}{\text{change in time}}$

velocity = speed, with a direction

Generalizing
given a function $f(x)$,

the average rate
of change of $f(x)$
with respect to x
between x_1 and x_2

$$= \frac{f(x_2) - f(x_1)}{x_2 - x_1} = \frac{\Delta f(x)}{\Delta x}$$

Instantaneous
rate of change
of $f(x)$
w.r.t. x at $x=a$

limit
 $x \rightarrow a$

$$\frac{f(x) - f(a)}{x - a}$$

Wrt = with respect to

I.r.o.c.
at $x=x_0$

$= \lim_{x \rightarrow x_0}$

$$\frac{f(x_1) - f(x_0)}{x_1 - x_0}$$

$= \lim_{h \rightarrow 0}$

$$\frac{f(x_0 + h) - f(x_0)}{h}$$



Let $y = x^2 + 1$

a) find the average rate of chg of y wrt x over $[3, 5]$.

$$= \frac{y(x=5) - y(x=3)}{5-3} = \frac{26-10}{2} = \frac{16}{2} = 8$$

b) find the instantaneous rate of chg of y wrt x at $x = -4$.

$$= \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a} = \lim_{x \rightarrow -4} \frac{(x^2 + 1) - ((-4)^2 + 1)}{x - (-4)} = \lim_{x \rightarrow -4} \frac{x^2 - 16}{x + 4}$$

$$= \lim_{x \rightarrow -4} \frac{(x-4)(x+4)}{(x+4)} = \lim_{x \rightarrow -4} (x-4) = -8$$

c) find $\lim_{x \rightarrow x_0} \frac{f(x) - f(x_0)}{x - x_0}$ at $x = x_0$

$$= \lim_{x \rightarrow x_0} \frac{(x^2 + 1) - (x_0^2 + 1)}{x - x_0}$$

$$= \lim_{x \rightarrow x_0} \frac{x^2 - x_0^2}{x - x_0} = \lim_{x \rightarrow x_0} \frac{(x - x_0)(x + x_0)}{(x - x_0)}$$

$$= \lim_{x \rightarrow x_0} x + x_0 = x_0 + x_0 = 2x_0$$

